Faculty of Health, Science and Technology

Syllabus Post graduatelevel

After completion of the course the student is expected to be able to

- identify continuoussymmetries in mechanical, quantum mechanical and quantum field theoretical systems and describe them with the help of the relevant mathematical structures

- define the notions of Lie group, Lie algebra, simple Lie algebra, **NK200**dy algebra, representation, module, highest weight module, enveloping algebra etc

- give a detailed account of central aspects of the structure theory and representation theory of Lie algebras, such as nilpotgensolvability, semisimplicity, irreducible representations, Verma modules, dualepresentations, tensor product, root and weight diagrams, the Killing form, the CartarWeyl basis etc

- describe the construction of affine Lie algebras via loop algebras and central extension

- describe the classification of fte-dimensional representations of complex semisimple Lie algebras, as well as compute their characters with the Weyl character formula

- give an account of the relation between Lie groups and Lie algebras

- present the classification of finitemensional complex simple Lie algebras and of affine Lie algebras, as well as summarize the most important steps of the proof of the classification

- explain the conection between real and complex semisimple Lie algebras

- apply computer programs for perfixing calculations for complex simple Lie algebras and their representations.

Course content

The course is taught in the form of lectures, exercise sessionstuce/lfof advanced topics both individually and in small groups, as well as literature studies.

The following topics are treated:

- definition as well as structure theory and representation theory of finite-dimensional Lie groups and Lie algebras as well as of Macody algebras

- the classification of finitedimensional complex simple Lie algebras and of affine Lie algebras, Carta Weyl bases, roots and simple roots, the Chevalley basis

- the Weyl group and root systems, root and weight diagrams, the enveloping algebra and Verma modules, irreducible highest weight modules, the Weyl and Waley character formulas

- dual representations, tensor product of representations, the Spacesler algorithm for decomposing tensor products

- Lie groups, relations between Lie groups and Lie algebras, Moartan theory

- Real semisimple Lie algebras

Reeding list See separate document.

Examination

The examination of the course is done in the form of homework exercises, written and

Reading list

Course name Lie Groups and Lie Algebras, 2FYS014, 7,5 hp/ECTSD(octoral studies)

The syllabus was approved by the Facoft Health, Science and Technology 201304-26 (Reg No: HNT 2013/22), and is valid from the Spring semester of 2013 at Karlstad University.

J. Fuchs and C. Schweigert: *Symmetries, Lie Algebras and Representations,* Cambridge University Press, ISBN 9780521541190

Reference literature:

P. Cvitanovic: Group Theory Classics Illustrated, http://www.cns.gatech.edu/GroupTheory