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Surendra Nepal, Department of Mathematics and Computer Science,
Karlstad University, Sweden.

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Models for capturing the penetration of a different concentration into rubber: Numerical analysis and simulation.

Abstract

Understanding the transport of diffusants into rubber plays an important role in forecasting the material's durability. In this regard, we study different models, conduct numerical analysis, and present simulation results that predict the evolution of diffusant penetration fronts. We employ a moving-boundary approach to model this phenomenon, utilizing a numerical scheme based on the Galerkin finite element method combined with the backward time discretization, to approximate the diffusant profile and the position of the penetration front. Both semi-discrete and fully discrete approximations are analyzed, demonstrating good agreement between numerical and theoretical convergence rates. Numerically approximated diffusant penetration front recovers well the experimental data. We introduce a random walk algorithm as an alternative tool to the finite element method, showing comparable results to the finite element approximation. In a multi-dimensional scenario, we consider a strongly coupled elliptic-parabolic two-scale system with nonlinear dispersion, describing the particle transport in a porous medium. We present two numerical schemes and compare them based on computational time and approximation errors. A precomputing strategy significantly improves computational efficiency.